

## 附錄一

由(4.17)式以及(4.18)式可知 $r_2^{NE}$ 、 $r_1^{NE}$ 為：

$$r_2^{NE} = \frac{1}{3} \left\{ \frac{A+B+2E+2F}{[(x_2-x_1)(1-\gamma hp - (1-\gamma)p) - z_2 + z_1]} \right\} + \frac{1}{3} b_1 z_1 + \frac{2}{3} b_2 z_2 + \frac{1}{3} c_1 + \frac{2}{3} c_2 \quad \text{-----(4.17)}$$

$$r_1^{NE} = -\frac{1}{3} \left\{ \frac{A+B+2E+2F}{[(x_2-x_1)(1-\gamma hp - (1-\gamma)p) - z_2 + z_1]} \right\} + \frac{A+B+E+F}{[(x_2-x_1)(1-\gamma hp - (1-\gamma)p) - z_2 + z_1]} + \frac{2}{3} b_1 z_1 + \frac{1}{3} b_2 z_2 + \frac{2}{3} c_1 + \frac{1}{3} c_2 \quad \text{-----(4.18)}$$

其中：

A=

$$(x_2 - x_1) \left\{ (a_1 x_1 + K_1) \left[ (1-\gamma)(1-hp)^2 + (1-p) \right] - (K_2 - K_1) \left[ (1-p) - hp(1-hp) \right] \right\}$$

B=

$$(-z_2 + z_1) \left\{ a_1 x_1 \left[ (1-hp) - \gamma p(1-h) \right] + (K_2 - K_1) \left[ -(1-hp) + \gamma p(1+h) \right] \right\}$$

E=

$$(x_2 - x_1) \left\{ [(1-p)(1+\gamma-hp)] [(a_2 x_2 + K_2) + (K_2 - K_1)] + \gamma (x_2 - x_1) [-\bar{y}p + \bar{y}hp] + [(x_2 - x_1)((\bar{y} - \bar{y}p) - z_2 + z_1)] [1 - \gamma hp] \right\}$$

F=

$$(-z_2 + z_1) \left\{ [-\gamma p + \gamma hp + 1 - hp] [(a_2 x_2 + K_2) + (K_2 - K_1)] + \gamma (x_2 - x_1) [-\bar{y}p + \bar{y}hp] + [(x_2 - x_1)((\bar{y} - \bar{y}hp) - z_2 + z_1)] \right\}$$

$$\begin{aligned} \therefore \frac{\partial r_2}{\partial x_1} &= \left( 6\gamma hp^2 K_1 + 12\gamma^2 hp^2 K_1 \right) x_1 + \left( -6\gamma hp^2 K_1 - 12\gamma^2 hp^2 K_1 \right) x_2 \\ &+ \left( 6hpK_1 - 6(hp)^2 K_1 + 9\gamma K_1 - 12\gamma hpK_1 + 3(hp)^2 K_2 - 12\gamma K_2 + 12\gamma pK_2 \right. \\ &- 6\gamma pK_1 - 3hp^2 K_2 + 3hp^2 K_1 + 6\gamma hpK_2 - 3K_1 + 9\gamma h^2 p^2 K_2 + 24\gamma^2 hp^2 K_2 \\ &- 15\gamma^2 h^2 p^2 K_2 - 12\gamma^2 hp^2 K_1 + 9\gamma^2 h^2 p^2 K_1 + 9\gamma p^2 K_2 - 24\gamma hp^2 K_2 \\ &\left. - 3\gamma p^2 K_1 + 12\gamma hp^2 K_1 - 9\gamma^2 p^2 K_2 + 3\gamma^2 p^2 K_1 \right) z_1 \\ &+ \left( -6hpK_1 + 6(hp)^2 K_1 - 9\gamma K_1 + 12\gamma hpK_1 - 3(hp)^2 K_2 + 12\gamma K_2 - 12\gamma pK_2 \right. \\ &+ 6\gamma pK_1 + 3hp^2 K_2 - 3hp^2 K_1 - 6\gamma hpK_2 + 3K_1 - 9\gamma h^2 p^2 K_2 - 24\gamma^2 hp^2 K_2 \\ &+ 15\gamma^2 h^2 p^2 K_2 + 12\gamma^2 hp^2 K_1 - 9\gamma^2 h^2 p^2 K_1 - 9\gamma p^2 K_2 + 24\gamma hp^2 K_2 \\ &\left. + 3\gamma p^2 K_1 - 12\gamma hp^2 K_1 + 9\gamma^2 p^2 K_2 - 3\gamma^2 p^2 K_1 \right) z_2 \end{aligned}$$

$$\begin{aligned}
& + (3a_1 - 6hpa_1 + 3(hp)^2a_1 - 3\gamma a_1 + 3\gamma hpa_1 + 3\gamma h^2p^2a_1 - 6\bar{y} + 12\bar{y}p \\
& - 12\gamma hp^2\bar{y} - 3\gamma h^3p^3a_1 + 3\gamma^2 hpa_1 - 6\gamma^2 h^2p^2a_1 + 3\gamma^2 h^3p^3a_1 - 6\gamma^2 \bar{y}hp^2 \\
& + 6\gamma \bar{y}hp + 6\gamma^2 \bar{y}h^2p^3 - 3pa_1 + 6hp^2a_1 - 3h^2p^3a_1 - 12\gamma hp^2a_1 + 6\gamma h^2p^3\bar{y} \\
& - 6\bar{y}p^2 + 6\gamma hp^3\bar{y} - 3\gamma^2 pa_1 + 6\gamma^2 hp^2a_1 - 3\gamma^2 h^2p^3a_1 + 6\gamma^2 \bar{y}p^2 - 6\gamma^2 hp^3\bar{y} \\
& - 6\gamma pa_1) x_1^2 \\
& + (3a_1 - 6hpa_1 + 3(hp)^2a_1 - 3\gamma a_1 + 3\gamma hpa_1 + 3\gamma h^2p^2a_1 - 6\bar{y} + 12\bar{y}p + 6\gamma hp\bar{y} \\
& - 12\gamma hp^2\bar{y} - 3\gamma h^3p^3a_1 + 3\gamma^2 hpa_1 - 6\gamma^2 h^2p^2a_1 + 3\gamma^2 h^3p^3a_1 + 6\gamma^2 \bar{y}h^2p^3 \\
& - 3pa_1 + 6hp^2a_1 - 3h^2p^3a_1 + 6\gamma pa_1 - 12\gamma hp^2a_1 + 6\gamma h^2p^3a_1 - 6\bar{y}p^2 \\
& - 6\gamma hp^3\bar{y} - 3\gamma^2 pa_1 + 6\gamma^2 hp^2a_1 - 3\gamma^2 h^2p^3a_1 + 6\gamma^2 \bar{y}p^2 - 6\gamma^2 hp^3\bar{y} \\
& - 6\gamma^2 pa_2 + 6\gamma p^2a_2 + 12hp^2a_2 - 6\gamma^2 hp^2\bar{y}) x_2^2 \\
& + (3a_1 - 3hpa_1 - 3\gamma pa_1 + 3\gamma hpa_1 - 12 + 12\gamma hp + 6\gamma \bar{y}p - 6\gamma \bar{y}hp - 6\bar{y} + 6\bar{y}hp \\
& + 6p - 6\gamma p) z_1^2 \\
& + (3a_1 - 3hpa_1 - 3\gamma pa_1 + 3\gamma hpa_1 - 12 + 12\gamma hp + 6\gamma \bar{y}p - 6\gamma \bar{y}hp - 6\bar{y} + 6\bar{y}hp \\
& + 6p - 6\gamma p) z_2^2 \\
& + (-12\gamma hp\bar{y} + 12\gamma hp^2\bar{y} + 6\gamma pa_2 - 6\gamma h^2p^3a_2 - 12\gamma \bar{y}hp^2 - 6a_1 + 12hpa_1 \\
& - 6(hp)^2a_1 + 6\gamma a_1 - 6\gamma hpa_1 + 12\bar{y} - 24\bar{y}p + 24\gamma hp^2\bar{y} + 6\gamma h^3p^3a_1 - 6\gamma^2 hpa_1 \\
& + 12\gamma^2 h^2p^2a_1 - 6\gamma^2 h^3p^3a_1 + 12\gamma^2 \bar{y} hp^2 - 12\gamma^2 \bar{y}h^2p^3 + 6pa_1 - 12hp^2a_1 \\
& + 6h^2p^3a_1 + 24\gamma hp^2a_1 - 12\gamma h^2p^3a_1 + 12\bar{y}p^2 - 12\gamma hp^3\bar{y} + 6\gamma^2 pa_1 \\
& - 12\gamma^2 hp^2a_1 + 6\gamma^2 h^2p^3a_1 - 24\gamma^2 \bar{y}p^2 + 12\gamma^2 hp^3\bar{y} - 12hp^2a_2 + 6\gamma hp^3a_2 \\
& + 12\gamma \bar{y}p^2 - 6\gamma pa_2) x_1x_2 \\
& + (-6a_1 + 12hpa_1 - 6(hp)^2a_1 + 6\gamma a_1 - 12\gamma hpa_1 + 6\gamma (hp)^2a_1 - 12\gamma \bar{y}p + 12\bar{y} \\
& - 12\bar{y}p + 12\gamma hp^2\bar{y}) x_1z_1 \\
& + (6a_1 - 12hpa_1 + 6(hp)^2a_1 - 6\gamma a_1 + 12\gamma hpa_1 - 6\gamma (hp)^2a_1 + 12\gamma \bar{y}p - 12\bar{y} \\
& + 12\bar{y}p - 12\gamma hp^2\bar{y}) x_1z_2 \\
& + (6a_1 - 9hpa_1 + 3(hp)^2a_1 - 3\gamma a_1 + 6\gamma hpa_1 + 12\gamma \bar{y}p - 12\bar{y} + 12\bar{y}p - 12\gamma hp^2\bar{y} \\
& - 6\gamma a_2 + 6\gamma pa_2 + 6\gamma^2 hp^2a_1 - 3\gamma^2 h^2p^2a_1 - 3pa_1 + 3hp^2a_1 + 3\gamma p^2a_1
\end{aligned}$$

$$\begin{aligned}
& -6\gamma hp^2a_1 - 3\gamma^2 p^2a_1 + 12\gamma^2 hp^2a_2 - 6\gamma^2 h^2p^2a_2 + 6\gamma h^2p^2a_2 + 6\gamma p^2a_2 \\
& - 12\gamma hp^2a_2 - 6\gamma^2 p^2a_2) x_2z_1 \\
& + (-6a_1 + 9hpa_1 - 3(hp)^2a_1 + 3\gamma a_1 - 6\gamma hpa_1 - 12\gamma \bar{y}p + 12\bar{y} - 12\bar{y}p \\
& + 12\gamma hp^2\bar{y} + 6\gamma a_2 - 6\gamma pa_2 - 6\gamma^2 hp^2a_1 + 3\gamma^2 h^2p^2a_1 + 3pa_1 - 3hp^2a_1 \\
& - 3\gamma p^2a_1 + 6\gamma hp^2a_1 + 3\gamma^2 p^2a_1 - 12\gamma^2 hp^2a_2 + 6\gamma^2 h^2p^2a_2 - 6\gamma h^2p^2a_2 \\
& - 6\gamma p^2a_2 + 12\gamma hp^2a_2 + 6\gamma^2 p^2a_2) x_2z_2 \\
& + (-6a_1 + 6hpa_1 + 6\gamma pa_1 - 6\gamma hpa_1 + 24 - 24\gamma hp - 12\gamma \bar{y}p + 12\gamma \bar{y}hp + 12\bar{y} \\
& - 12\bar{y}hp - 12p + 12\gamma p) z_1z_2 = 0 \text{-----}(4.20)
\end{aligned}$$

