

- 一. 求 $y = (x^2 + 4)^3 (3x - 2)^2$ 之導數 (10%)
- 二. 設 $x^2 + 2xy + 3y^2 = 1$, 求 $\frac{dy}{dx}$ 及 $\frac{d^2y}{dx^2}$ (10%)
- 三. 以直尺量一圓之直徑為 6.4 吋, 若量度之可能誤差為 0.05 吋, 則計算圓面積之最大誤差為何? (10%)
- 四. 試求曲線 $x = t^2 - 2t$, $y = 1 - t^2$ 之垂直切線之切點 (10%)
- 五. 某旅行社估計每週代售機位 x 個之成本以元計為
- $$C(x) = x^3 - 3x^2 - 80x + 500$$
- 每個機位之售價為 2800 元, 試問每週代售機位若干個可利潤最大? 又最大利潤為何? (10%)

六. Evaluate $\int_0^{\infty} \int_0^1 ye^{y^2-x} dy dx$. (10%)

七. Determine the convergence or divergence of $\int_{-\infty}^0 (x+1)e^x dx$. (10%)

八. Suppose a company has a monthly revenue function $R(t) = 4t^2e^{-t/2} + 50$. (R in thousands and t is in months.) What is the average monthly revenue during the first quarter, $0 \leq t \leq 4$? (15%)

- 九. If the time required for a person to learn to use a new computer software program, is described by the probability density function

$$f(t) = \frac{15}{128} t\sqrt{4-t}, \quad [0, 4]$$

find the probability that a person will learn to use the program in less than three hours.

一、Three coins, one dollar, half-dollar and quarter, are tossed once.(25%)

(1) Describe the sample space Ω . (5%)

(2) If the coins are fair, what will be the probabilities associated with each point of Ω ? (5%)

Suppose that the rules of the game are that you win every coin that falls "heads". We define X to be a random variable representing your total winnings in cents.

(Note : one dollar = 100 cents, half-dollar = 50 cents, quarter = 25 cents)

(3) Exhibit the relationship between X and the points of Ω . (5%)

(4) Find the probability density function of X , and identify it as one of our standard distributions.(10%)

二、A coin is tossed 200 times, and "heads" shows 116 times. Define p to be the unknown probability of appearing "heads".(25%)

(1) Construct a 95% confidence interval for p . (5%)

If you believe this coin is fair,

(2) State the null and the alternative hypotheses that you would choose for a statistical test. (5%)

(3) Conduct the test and state your conclusions. ($\alpha=0.05$) (10%)

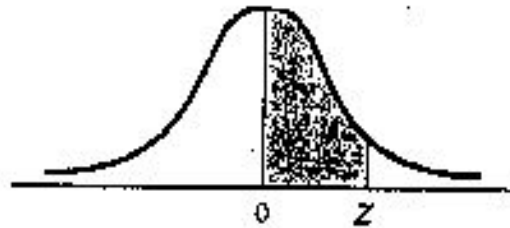
(4) Find the p -value for the above test. (5%)

(第一頁 · 共四頁)

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Entry represents area under the standardized normal distribution from the mean to Z

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0278	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1735	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2089	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3316	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4346	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4655	.4664	.4671	.4678	.4685	.4693	.4699	.4706
1.9	.4713	.4718	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4958	.4959	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4985	.4986
3.0	.4986	.4986	.4987	.4987	.4988	.4988	.4988	.4989	.4989	.4990
3.1	.4990	.4990	.4991	.4991	.4991	.4991	.4992	.4992	.4992	.4992
3.2	.4993	.4993	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995
3.3	.4995	.4995	.4995	.4995	.4995	.4995	.4995	.4995	.4995	.4995
3.4	.4996	.4996	.4996	.4996	.4996	.4996	.4996	.4996	.4996	.4996
3.5	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997
3.6	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997
3.7	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998
3.8	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998
3.9	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999

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(三)某酒店最近的一個月內每日之服務顧客人數(X)與當日營業收入(Y)，單位為百元，之迴歸分析結果(SAS 報表)

Source	DF	Sum of Squares	Mean Square	F Value	Prob > F
Model	1	37.65058	37.65058	10.807	0.0028
Error	6	14.30342	2.38390		
Total	7	51.95400			

Root MSE	R-Square	Adj R-Sq	F Value
1.54369	0.7248	0.6746	
DF	Mean	St Dev	
1	15.91365		

Variable	DF	Parameter Estimate	Standard Error	t for H0: Parameter=0	Prob > t
INTERCEPT	1	-5.803350	3.24859918	-1.802	0.1479
X (顧客人數)	1	0.233382	0.05325495	4.388	0.0027

6分 (1)列出迴歸方程式並解釋其意義。

7分 (2)以 $\alpha = 0.05$ 檢定服務顧客人數與當日營業收入是否有顯著的關係(請列出無與對立假設)

(四)以三種不同溫度(A,B,C)保存啤酒 15 天，得其可以保存之時間(單位為日)如下表所列：

時 間	溫 度		
	A	B	C
第 一 天	25	20	16
	24	19	18
	18	31	19
第 二 天	21	22	21
	23	20	18
	22	21	19
總 數	111	102	92
平均數	37.0	34.0	30.7

10分 (1)試建立變異數分析表。

10分 (2)以 $\alpha = 0.05$ 檢定不同之溫度下，啤酒之保存時間是否有顯著之差異(請列出無與對立假設)

15分 (五)某廠的隨機抽取 18 位員工，組裝廠內所 產之越野自行車，其組裝時間(單位為分鐘)分別如下：

108, 88, 86, 90, 66, 26, 39, 55, 88, 41, 54, 70, 66, 88, 72, 76, 73, 93。試以 $\alpha = 0.01$ 檢定組裝時間之單位數是否小於 90 分鐘。(請列出無與對立假設)

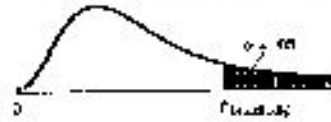
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TABLE E.8 Critical Values of F

For a particular combination of numerator and denominator degrees of freedom, every entry represents the critical value of F corresponding to a specified upper tail area.



Denominator df	Numerator df																			
	1	2	3	4	5	6	7	8	9	10	15	20	25	30	40	50	60	80	100	
1	161.4	199.5	215.7	224.6	231.0	235.0	238.0	240.0	241.5	242.8	243.8	244.6	245.3	245.9	246.5	247.0	247.5	247.9	248.3	248.6
2	18.51	18.00	17.58	17.24	16.97	16.74	16.58	16.46	16.36	16.28	16.21	16.15	16.10	16.05	16.01	15.97	15.94	15.91	15.88	15.86
3	16.17	15.53	15.10	14.75	14.47	14.24	14.06	13.92	13.81	13.72	13.65	13.59	13.54	13.50	13.46	13.43	13.40	13.37	13.35	13.33
4	14.52	13.77	13.33	12.97	12.68	12.44	12.25	12.10	12.00	11.91	11.84	11.78	11.73	11.69	11.65	11.62	11.59	11.57	11.55	11.53
5	13.27	12.41	11.96	11.59	11.29	11.04	10.84	10.68	10.58	10.49	10.42	10.36	10.31	10.27	10.23	10.20	10.17	10.15	10.13	10.11
6	12.22	11.25	10.79	10.41	10.10	9.84	9.63	9.46	9.36	9.27	9.20	9.14	9.09	9.05	9.01	8.98	8.95	8.93	8.91	8.89
7	11.33	10.25	9.78	9.39	9.07	8.80	8.58	8.40	8.30	8.21	8.14	8.08	8.03	8.00	7.96	7.93	7.91	7.89	7.87	7.85
8	10.57	9.38	8.90	8.50	8.17	7.89	7.66	7.47	7.37	7.28	7.21	7.15	7.10	7.06	7.03	7.00	6.98	6.96	6.94	6.92
9	9.91	8.61	8.12	7.71	7.37	7.08	6.84	6.64	6.54	6.45	6.38	6.32	6.27	6.23	6.20	6.17	6.15	6.13	6.11	6.09
10	9.33	7.92	7.42	7.00	6.65	6.35	6.10	5.90	5.80	5.71	5.64	5.58	5.53	5.49	5.46	5.43	5.41	5.39	5.37	5.35
15	7.76	6.24	5.73	5.30	4.94	4.63	4.37	4.16	4.06	3.97	3.90	3.84	3.79	3.75	3.72	3.69	3.67	3.65	3.63	3.61
20	6.90	5.37	4.85	4.41	4.04	3.73	3.46	3.25	3.15	3.06	2.99	2.93	2.88	2.84	2.81	2.78	2.76	2.74	2.72	2.70
25	6.35	4.81	4.28	3.83	3.45	3.14	2.86	2.65	2.55	2.46	2.39	2.33	2.28	2.24	2.21	2.18	2.16	2.14	2.12	2.10
30	5.95	4.40	3.86	3.40	3.01	2.70	2.41	2.20	2.10	2.01	1.94	1.88	1.83	1.79	1.76	1.73	1.71	1.69	1.67	1.65
40	5.28	3.72	3.17	2.70	2.30	1.99	1.69	1.48	1.38	1.29	1.22	1.16	1.11	1.07	1.04	1.01	0.99	0.97	0.95	0.93
50	4.84	3.27	2.71	2.24	1.83	1.52	1.21	1.00	0.90	0.81	0.74	0.68	0.63	0.59	0.56	0.53	0.51	0.49	0.47	0.45
60	4.50	2.93	2.36	1.88	1.47	1.15	0.84	0.63	0.53	0.44	0.37	0.31	0.26	0.22	0.19	0.17	0.15	0.13	0.11	0.09
80	4.07	2.50	1.92	1.44	1.03	0.71	0.40	0.19	0.09	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
100	3.74	2.17	1.58	1.10	0.69	0.37	0.16	0.05	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

TABLE E.10 Lower and Upper Critical Values W of Wilcoxon Signed-Rank Test

n	One-Tailed: $\alpha = .25$		$\alpha = .10$		$\alpha = .05$		$\alpha = .025$		$\alpha = .01$	
	Lower	Upper	Lower	Upper	Lower	Upper	Lower	Upper	Lower	Upper
2	0.15	1.85	0.25	1.75	0.40	1.60	0.50	1.50	0.75	1.25
3	0.15	2.85	0.25	2.75	0.40	2.60	0.50	2.50	0.75	2.25
4	0.25	3.75	0.35	3.65	0.50	3.50	0.60	3.40	0.85	3.15
5	0.35	4.65	0.45	4.55	0.60	4.40	0.70	4.30	1.00	4.00
6	0.45	5.55	0.55	5.45	0.70	5.30	0.80	5.20	1.15	4.85
7	0.55	6.45	0.65	6.35	0.80	6.20	0.90	6.10	1.30	4.70
8	0.65	7.35	0.75	7.25	0.90	7.10	1.00	7.00	1.45	4.55
9	0.75	8.25	0.85	8.15	1.00	8.00	1.10	7.90	1.60	4.40
10	0.85	9.15	0.95	9.05	1.10	8.90	1.20	8.80	1.75	4.25
11	0.95	10.05	1.05	9.95	1.20	9.80	1.30	9.70	1.90	4.10
12	1.05	10.95	1.15	10.85	1.30	10.70	1.40	10.60	2.05	3.95
13	1.15	11.85	1.25	11.75	1.40	11.60	1.50	11.50	2.20	3.80
14	1.25	12.75	1.35	12.65	1.50	12.50	1.60	12.40	2.35	3.65
15	1.35	13.65	1.45	13.55	1.60	13.40	1.70	13.30	2.50	3.50
16	1.45	14.55	1.55	14.45	1.70	14.30	1.80	14.20	2.65	3.35
17	1.55	15.45	1.65	15.35	1.80	15.20	1.90	15.10	2.80	3.20
18	1.65	16.35	1.75	16.25	1.90	16.10	2.00	16.00	2.95	3.05
19	1.75	17.25	1.85	17.15	2.00	17.00	2.10	16.90	3.10	2.90
20	1.85	18.15	1.95	18.05	2.10	17.90	2.20	17.80	3.25	2.75

Source: Adapted from Table E of F. Wilcoxon and R. A. Wilco, Some Newer Aspects of Statistical Procedures (Fairfax, N.Y.: Lakeside Laboratories, 1964), by permission of the American Cynology Company.

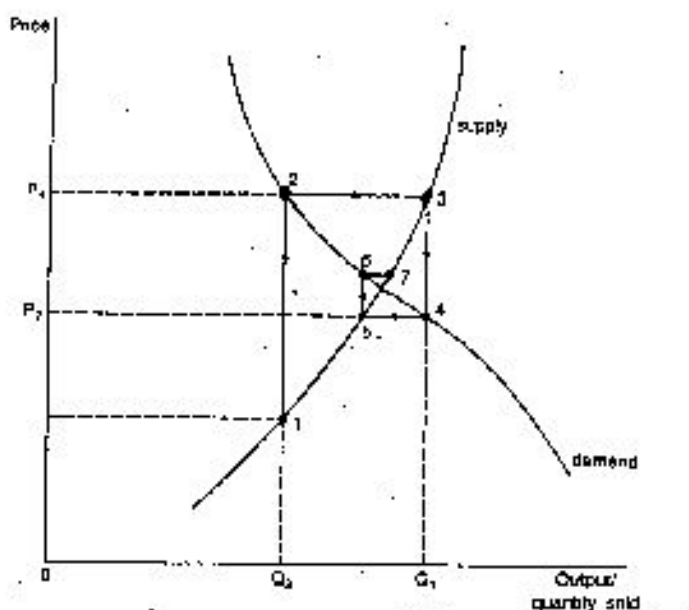
I. 名詞解釋

1. Substitution Effect (替代效果) (10分)
2. Pareto Efficiency (10分)
3. 乘數效應 (Multiplier) (7%)
4. 漏耗 (Leakage) (7%)
5. 在外性 (Externality) (7%)

II. 简答题

1. 請說明影響需求曲線變動(movement along a demand curve)的因子以及影響需求變動(shift of the demand curve)的因子 (10分)

2. 請簡介下圖 (14%)



III. 中論題

1. 宜蘭縣的地方人士針對龜山島的開發提出以下三個建議案

- A. 高度開發為觀光賭場
- B. 中度開發為海濱活動休閒度假的據點
- C. 低度開發：僅供保育及生態研究

宜蘭縣政府請你以經濟學的角度來分析三個建議案對於宜蘭縣帶來的總體效益及影響為何？請說明你將如何來評估？

(20分)

2. 最近臺幣大幅貶值，試問其對臺灣的 Inbound 及 Outbound 旅遊有何影響。請申論之。(15%)