

- 一、 For some methods, the cost of purifying a gallon of water to a purity of  $x$  percent is

$$C(x) = \frac{2}{100-x} \quad \text{for } 80 < x < 100$$

dollars. Find the rate of change of purification costs when purity is:  
a. 90% (5分) b. 98%. (5分)

- 二、 a. Find  $\frac{d^2}{dx^2} \left( \frac{x^2+1}{x} \right)$ . (5分)      b. If  $f(x) = \frac{1}{\sqrt{x}}$ , find  $f''\left(\frac{1}{4}\right)$ . (5分)

- 三、 It costs the American Automobile Company \$5000 to produce each automobile, and fixed costs (rent and other costs that do not depend on the amount of production) are \$20,000 per week. The company's price function is  $p = 19,000 - 70x$ , where  $p$  is the price at which exactly  $x$  cars will be sold.

- a. How many cars should be produced each week to maximize profit? (5分)  
b. For what price should they be sold? (5分)  
c. What is the company's maximum profit? (5分)

- 四、 A study of urban pollution predicts that sulfur oxide emissions in a city will be  $S = 2 + 20x + 0.1x^2$  tons, where  $x$  is the population (in thousands). The population of the city  $t$  years from now is expected to be  $x = 800 + 20\sqrt{t}$  thousand people. Find how rapidly sulfur oxide pollution will be increasing 4 years from now. (15分)

- 五、 求  $\lim_{b \rightarrow \infty} \frac{1}{b} \int_0^b \sqrt{2+\sqrt{2+td}} \cdot dt$ . (10分)

- 六、 利用  $\pi = 4 \int_0^1 \frac{1}{1+x^2} dx$  及辛普森法則(Simpson's rule), 將區間  $[0, 1]$  分為四等分, 求  $\pi$  的近似值(算至小數第四位). (10分)

- 七、 求當線  $y = x^2$  與直線  $y = x$  所圍區域面積. (10分)

- 八、 某公司生產兩種產品 X 與 Y, 生產  $x$  單位與產品 Y 生產  $y$  單位時的總成本函數為  $C(x, y) = 25x + 36y + \frac{400}{x} + \frac{144}{y}$ . 若欲總成本為最低, 試問此兩種產品 X 與 Y 各應生產若干單位? (10分)

- 九、 求下列積分:

(a).  $\int \frac{1}{x^2 - a^2} dx$ . (5分)

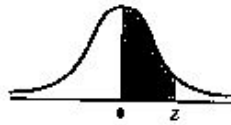
(b).  $\int \log_n x dx$ . (5分)

(第一頁, 共一頁)

1. A study of a major metropolitan hospital revealed that of every 100 medications prescribed or dispensed, 1 was in error; but, only 1 in 500 resulted in an error that caused significant problems for the patient. It is known that the hospital prescribes and dispenses 60,000 medications per year.
- (5%) a. What is the expected number of errors per year at this hospital? The expected number of significant errors per year?
- (5%) b. Within what limits would you expect the number of significant errors per year to fall?
- (5%) c. What assumptions did you need to make in order to answer these questions?
- (10%) 2. In August 1995 the Gallup organization conducted interviews with a random sample of 1,002 people who operate businesses in their homes. The most common reason given for starting a home business was wanting to be one's own boss (170 respondents); being laid off was the least common reason (30 respondents). Is the sample size large enough to construct a valid confidence interval for the proportion of home business operators who started their business because they were laid off? Justify your answer.
3. An auditor for the Internal Revenue Service is selecting a sample of six tax returns from persons in a particular profession for possible audit. If two or more of these indicate "improper" deductions, the entire group (population) of 100 tax returns will be audited.
- (10%) a. What is the probability that the entire group will be audited if the true number of improper returns in the population is 25?
- (5%) b. Discuss the differences in your results depending on the true number of improper returns in the population.
- (10%) 4. Sally is 67 inches tall and weighs 135 pounds. If the heights of women are normally distributed with  $\mu = 65$  inches and  $\sigma = 2.5$  inches and if the weights of women are normally distributed with  $\mu = 125$  pounds and  $\sigma = 10$  pounds, determine whether Sally's more unusual characteristic is her height or her weight. Discuss.

( 第一頁 . 共五頁 )

Table E.2a The Standardized Normal Distribution

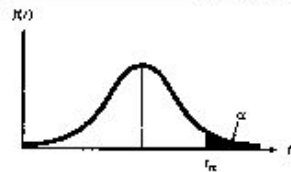


Entry represents area under the standardized normal distribution from the mean to Z

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2421	.2454	.2486	.2518	.2549
0.7	.2580	.2612	.2643	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2938	.2967	.2995	.3023	.3051	.3079	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3829
1.2	.3849	.3868	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4685	.4692	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4915
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4935
2.5	.4937	.4939	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4958	.4959	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4986	.4986	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990
3.1	.4990	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4995	.4995	.4995	.4995	.4996
3.3	.4996	.4996	.4997	.4997	.4997	.4998	.4998	.4998	.4998	.4999
3.4	.4999	.4999	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000
3.5	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000
3.6	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000
3.7	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000
3.8	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000

( 第二頁 . 共五頁 )

TABLE VI Critical Values of  $t$



$\alpha$	$t_{.99}$	$t_{.95}$	$t_{.90}$	$t_{.85}$	$t_{.80}$	$t_{.75}$	$t_{.70}$
1	3.078	6.314	12.706	31.821	63.657	118.31	636.62
2	1.986	2.920	4.303	6.965	9.925	22.326	31.598
3	1.638	2.353	3.182	4.541	5.841	10.213	12.924
4	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	1.476	2.015	2.571	3.363	4.032	5.893	6.869
6	1.440	1.943	2.447	3.142	3.707	5.208	5.959
7	1.415	1.895	2.365	2.996	3.499	4.783	5.408
8	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	1.383	1.833	2.262	2.821	3.280	4.297	4.781
10	1.372	1.812	2.228	2.761	3.169	4.144	4.587
11	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	1.350	1.771	2.160	2.650	3.013	3.852	4.221
14	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	1.328	1.729	2.093	2.539	2.861	3.579	3.885
20	1.325	1.725	2.086	2.528	2.845	3.552	3.850
22	1.323	1.721	2.080	2.518	2.831	3.527	3.819
24	1.321	1.717	2.074	2.508	2.819	3.503	3.792
26	1.319	1.714	2.069	2.500	2.807	3.483	3.767
28	1.318	1.711	2.064	2.492	2.797	3.467	3.745
30	1.317	1.708	2.060	2.485	2.787	3.450	3.725
35	1.315	1.706	2.056	2.479	2.779	3.435	3.707
40	1.314	1.703	2.052	2.473	2.771	3.421	3.690
45	1.313	1.701	2.048	2.467	2.765	3.408	3.674
50	1.311	1.699	2.045	2.462	2.758	3.396	3.659
60	1.310	1.697	2.042	2.457	2.750	3.385	3.646
70	1.309	1.694	2.02	2.453	2.704	3.377	3.551
80	1.296	1.673	2.000	2.390	2.660	3.332	3.440
100	1.289	1.658	1.980	2.374	2.617	3.160	3.373
$\infty$	1.282	1.645	1.960	2.326	2.576	3.090	3.291

Source: This table is reproduced with the kind permission of the Trustees of Biometrika from E. S. Pearson and H. O. Hartley (eds.), *The Biometrika Tables for Statisticians*, Vol. 1, 3rd ed., Biometrika, 1966.

( 第三頁 共五頁 )

4. It is suspected that the environment temperature in which batteries are activated affects their activated life. Thirty homogeneous batteries are tested, six at each five temperatures, and the data are shown below:(25%)

	Temperature(°C)				
	0	25	50	75	100
Activated Life (seconds)	55	60	70	72	65
	55	61	72	72	66
	57	60	73	72	60
	54	60	68	70	64
	54	60	77	68	63
	56	60	77	69	65

- (1) What is the factor? What are the treatments? (8%)
- (2) Do the data provide sufficient evidence to indicate differences among five temperatures? (State the ANOVA table and draw conclusions.  $\alpha=0.05$ ) (Note:  $MSE=4.5133$ ,  $F\text{-ratio}=70.27$ ,  $p\text{-value}=0.0001$ ) (10%)
- (3) Give the necessary assumptions for the above analysis of variance. (7%)

5. A portion of a multiple regression computer output is shown below:(25%)

Predictor	Coef	Stdev. Coef
Constant	0.4706	0.5433
X <sub>1</sub>	0.0035628	0.0007350
X <sub>2</sub>	0.0001576	0.0008514

s = 0.5018

Analysis of Variance

SOURCE	DF	SS	MS
Regression	2		
Error	97		
Total	99		

SOURCE	DF	SEQ SS
X	1	7.5051
X <sub>2</sub>	1	0.0086

(regression model:  $E(Y) = \beta_0 + \beta_1 X_1 + \beta_2 X_2$ )

- (1) Give the prediction equation for the multiple regression analysis. (5%)
- (2) Do the data provide sufficient evidence to indicate that X<sub>1</sub> and X<sub>2</sub> contribute information for the prediction of Y? Test using  $\alpha=0.05$  (10%)
- (3) What is the value of R<sup>2</sup> (R-square) for the analysis? (5%)
- (4) What is the value of residual associated with the observed y-value=2.3, X<sub>1</sub>-value=454, X<sub>2</sub>-value=471? (5%)

( 第四頁 共五頁 )

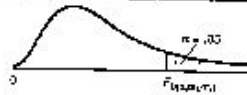
中國文化大學八十八學年度碩士班入學考試

所(組)別：國際企業管理研究所

考試科目：統計學

Critical Values of F

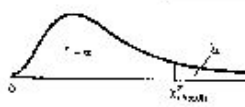
For a particular combination of numerator and denominator degrees of freedom, the critical value of F corresponding to a specified upper tail area is



Degrees of Freedom	Denominator df																				
	1	2	3	4	5	6	7	8	9	10	15	20	25	30	40	50	60	70	80	90	100
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5	241.9	243.1	244.1	245.0	245.8	246.5	247.1	247.7	248.2	248.6	249.0	249.4
2	18.51	18.00	17.59	17.25	16.97	16.72	16.50	16.31	16.15	16.01	15.88	15.76	15.65	15.55	15.45	15.36	15.27	15.19	15.11	15.03	14.95
3	10.13	9.58	9.19	8.86	8.58	8.34	8.13	7.94	7.78	7.64	7.51	7.39	7.28	7.18	7.09	7.00	6.91	6.83	6.75	6.67	6.59
4	7.71	7.09	6.72	6.40	6.13	5.89	5.68	5.49	5.33	5.19	5.06	4.94	4.83	4.74	4.65	4.57	4.49	4.41	4.33	4.25	4.17
5	6.58	5.89	5.54	5.22	4.95	4.71	4.50	4.31	4.15	4.01	3.88	3.76	3.65	3.56	3.47	3.39	3.31	3.23	3.15	3.07	2.99
6	5.95	5.20	4.86	4.54	4.27	4.03	3.82	3.63	3.47	3.33	3.20	3.08	2.97	2.88	2.80	2.72	2.64	2.56	2.48	2.40	2.32
7	5.49	4.68	4.35	4.03	3.76	3.52	3.31	3.12	2.96	2.82	2.69	2.57	2.46	2.37	2.29	2.21	2.13	2.05	1.97	1.89	1.81
8	5.12	4.25	3.92	3.60	3.33	3.09	2.88	2.69	2.53	2.39	2.26	2.14	2.03	1.94	1.86	1.78	1.70	1.62	1.54	1.46	1.38
9	4.81	3.88	3.55	3.23	2.96	2.72	2.51	2.32	2.16	2.02	1.89	1.77	1.66	1.57	1.49	1.41	1.33	1.25	1.17	1.09	1.01
10	4.54	3.56	3.23	2.91	2.64	2.40	2.19	2.00	1.84	1.70	1.57	1.45	1.34	1.25	1.17	1.09	1.01	0.93	0.85	0.77	0.69
11	4.31	3.28	2.95	2.63	2.36	2.12	1.91	1.72	1.56	1.42	1.29	1.17	1.06	0.97	0.89	0.81	0.73	0.65	0.57	0.49	0.41
12	4.10	3.03	2.70	2.38	2.11	1.87	1.66	1.47	1.30	1.16	1.03	0.91	0.80	0.71	0.63	0.55	0.47	0.39	0.31	0.23	0.15
13	3.91	2.80	2.47	2.15	1.88	1.64	1.43	1.24	1.07	0.93	0.80	0.68	0.57	0.48	0.40	0.32	0.24	0.16	0.08	0.00	0.00
14	3.74	2.59	2.26	1.94	1.67	1.43	1.22	1.03	0.86	0.72	0.59	0.47	0.36	0.27	0.19	0.11	0.03	0.00	0.00	0.00	0.00
15	3.59	2.40	2.07	1.75	1.48	1.24	1.03	0.84	0.67	0.53	0.40	0.28	0.17	0.08	0.00	0.00	0.00	0.00	0.00	0.00	0.00
16	3.45	2.22	1.89	1.57	1.30	1.06	0.85	0.66	0.49	0.35	0.22	0.10	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
17	3.32	2.05	1.72	1.40	1.13	0.89	0.68	0.49	0.32	0.18	0.05	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
18	3.20	1.89	1.56	1.24	0.97	0.73	0.52	0.33	0.16	0.02	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
19	3.09	1.79	1.46	1.14	0.87	0.63	0.42	0.23	0.06	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
20	2.99	1.70	1.37	1.05	0.78	0.54	0.33	0.14	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
25	2.70	1.41	1.08	0.76	0.49	0.25	0.04	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
30	2.55	1.25	0.92	0.60	0.33	0.09	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
40	2.30	1.00	0.67	0.35	0.08	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
50	2.15	0.85	0.52	0.20	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
60	2.05	0.75	0.42	0.10	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
70	1.98	0.68	0.35	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
80	1.92	0.62	0.29	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
90	1.87	0.58	0.25	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
100	1.83	0.55	0.22	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

Critical Values of  $\chi^2$

For a particular number of degrees of freedom, the critical value of  $\chi^2$  corresponding to a specified upper tail area is



Degrees of Freedom	Upper Tail Areas (a)										
	0.10	0.05	0.025	0.01	0.005	0.001	0.05	0.01	0.005	0.001	0.0005
1	2.706	3.841	5.024	6.635	7.879	10.828	2.706	3.841	5.024	6.635	7.879
2	1.635	2.771	3.828	5.991	7.378	10.597	1.635	2.771	3.828	5.991	7.378
3	1.213	2.366	3.413	5.541	6.928	10.243	1.213	2.366	3.413	5.541	6.928
4	0.975	2.000	3.000	5.192	6.581	9.886	0.975	2.000	3.000	5.192	6.581
5	0.854	1.753	2.750	4.959	6.386	9.633	0.854	1.753	2.750	4.959	6.386
6	0.788	1.626	2.603	4.753	6.193	9.488	0.788	1.626	2.603	4.753	6.193
7	0.737	1.535	2.467	4.575	6.024	9.353	0.737	1.535	2.467	4.575	6.024
8	0.699	1.450	2.338	4.415	5.871	9.236	0.699	1.450	2.338	4.415	5.871
9	0.670	1.380	2.215	4.266	5.729	9.133	0.670	1.380	2.215	4.266	5.729
10	0.646	1.320	2.093	4.129	5.591	9.033	0.646	1.320	2.093	4.129	5.591
11	0.626	1.265	1.972	3.993	5.457	8.936	0.626	1.265	1.972	3.993	5.457
12	0.608	1.214	1.853	3.860	5.327	8.842	0.608	1.214	1.853	3.860	5.327
13	0.592	1.166	1.736	3.730	5.200	8.751	0.592	1.166	1.736	3.730	5.200
14	0.578	1.121	1.621	3.602	5.076	8.662	0.578	1.121	1.621	3.602	5.076
15	0.564	1.078	1.508	3.478	4.954	8.575	0.564	1.078	1.508	3.478	4.954
16	0.551	1.037	1.397	3.357	4.834	8.490	0.551	1.037	1.397	3.357	4.834
17	0.539	0.997	1.288	3.239	4.716	8.407	0.539	0.997	1.288	3.239	4.716
18	0.528	0.959	1.181	3.124	4.600	8.326	0.528	0.959	1.181	3.124	4.600
19	0.518	0.923	1.076	3.011	4.486	8.246	0.518	0.923	1.076	3.011	4.486
20	0.509	0.889	0.973	2.900	4.374	8.167	0.509	0.889	0.973	2.900	4.374
21	0.500	0.856	0.872	2.791	4.264	8.089	0.500	0.856	0.872	2.791	4.264
22	0.492	0.824	0.773	2.684	4.156	8.013	0.492	0.824	0.773	2.684	4.156
23	0.484	0.793	0.675	2.579	4.050	7.938	0.484	0.793	0.675	2.579	4.050
24	0.477	0.763	0.578	2.475	3.946	7.864	0.477	0.763	0.578	2.475	3.946
25	0.470	0.734	0.482	2.373	3.844	7.791	0.470	0.734	0.482	2.373	3.844
26	0.464	0.705	0.387	2.272	3.743	7.719	0.464	0.705	0.387	2.272	3.743
27	0.458	0.677	0.293	2.173	3.643	7.648	0.458	0.677	0.293	2.173	3.643
28	0.452	0.649	0.200	2.075	3.544	7.578	0.452	0.649	0.200	2.075	3.544
29	0.447	0.622	0.107	1.978	3.446	7.509	0.447	0.622	0.107	1.978	3.446
30	0.442	0.595	0.015	1.882	3.349	7.440	0.442	0.595	0.015	1.882	3.349

( 第五頁, 共五頁 )