

$$20\% - y' = 1 + y^2$$

① 求 y 曲線族

② 求 y 正交曲線族

$$40\% = \text{ODE}$$

$$\textcircled{a} \quad e^{-2\theta} dr - 2r e^{-2\theta} d\theta = 0, \text{ 求通解}$$

$$\textcircled{b} \quad y' + y \tan x = \sin 2x, \text{ 求通解}$$

$$\textcircled{c} \quad x^2 y'' - 4x y' + 6y = 0, \text{ 求通解}$$

$$\textcircled{d} \quad y'' + ay' + by = 0, \quad a, b \text{ 常数}$$

若存在 oscillation solution, 則 a, b 要
滿足何條件?

20% 三. 向量

$$\textcircled{a} \quad f = f(x, y, z) \text{ 純量函數, 若 } \vec{v} = \nabla f \\ \text{證明 } \nabla \times \vec{v} = 0$$

$$\textcircled{b} \quad \text{向量函數 } \vec{F} = x\vec{i} + y\vec{j} + z\vec{k}. \text{ 若 } \vec{F} = \nabla f \\ \text{試求 } f$$

20% 四. Legendre polynomials

$$P_2(x) = \frac{1}{2}(3x^2 - 1), \quad P_3(x) = \frac{1}{2}(5x^3 - 3x)$$

$$\overline{\text{正}} \wedge P_2(x) \wedge P_3(x) \quad \{ \text{正}\}$$